

# CMOS Systems & Interfaces for Sub-deg/hr Microgyroscopes

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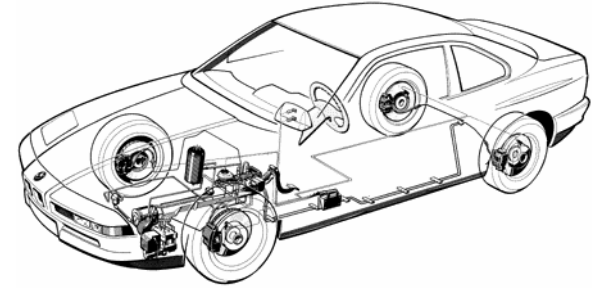


# Outline

- ❑ Mode-Matched Tuning Fork Gyroscope (M<sup>2</sup>-TFG)
- ❑ System level considerations for MEMS interfacing
- ❑ Transimpedance amplifier (TIA) front-ends
- ❑ T-network TIA
- ❑ Circuit implementation of gyro sub-systems
- ❑ Interfacing results
- ❑ Conclusions

# Market Demands

- Automotive Applications



- Consumer Applications

- Image stabilization in digital cameras
- Smart user interfaces
- Short range navigation



- High-Performance Applications

- Aerospace
- Defense
- Precision inertial measurement units



# Performance Classes

	<i>Rate Grade</i>	<i>Navigation Grade</i>
<i>Bias drift</i>	10 to 1000 deg/hr	0.01 to 1 deg/hr
<i>Angle random walk</i>	> 0.5 deg/ $\sqrt{\text{hr}}$	< 0.005 deg/ $\sqrt{\text{hr}}$
<i>Scale factor accuracy</i>	0.1% to 1%	< 10 ppm
<i>Full scale range</i>	50 - 1000 deg/sec	~ 500 deg/sec
<i>Bandwidth</i>	> 70 Hz	~10Hz

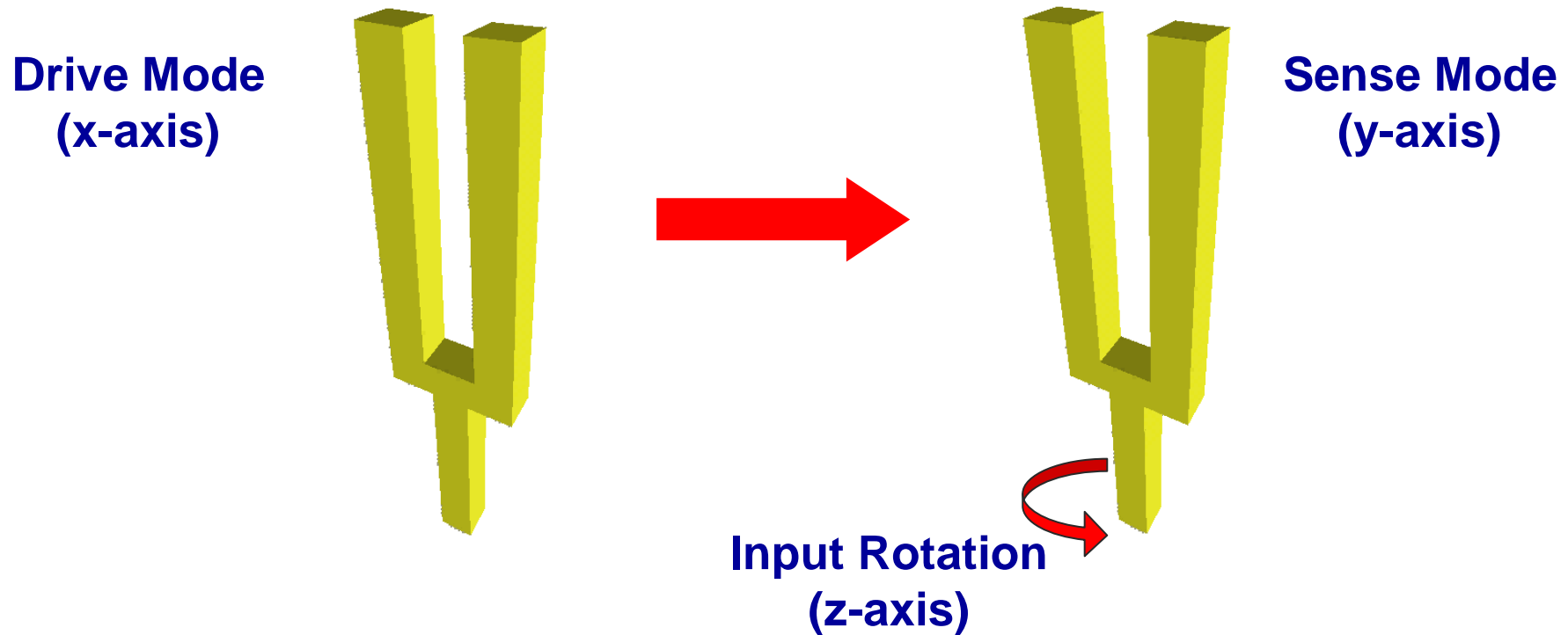
$\text{°/hr}/\sqrt{\text{Hz}}$   
Resolution

$\text{°}/\sqrt{\text{hr}}$   
Angle Random Walk

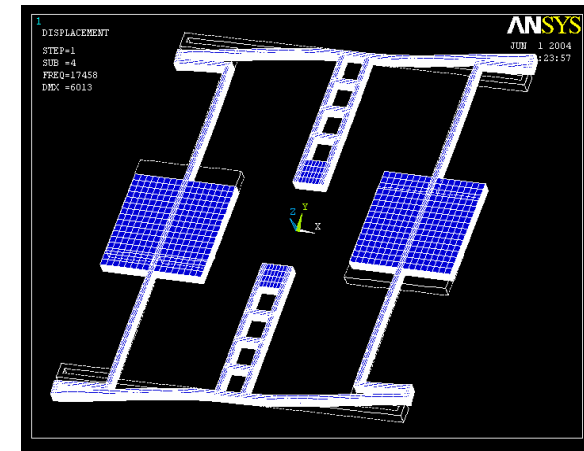
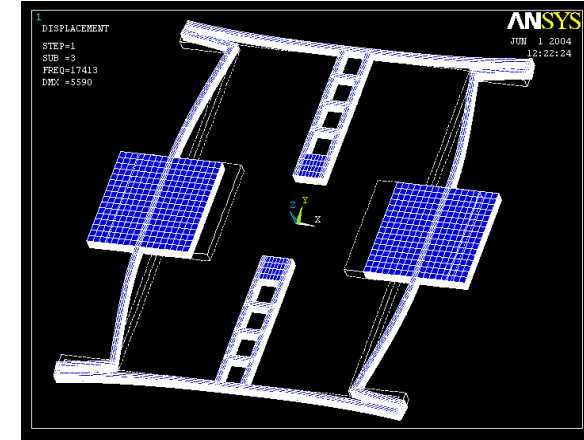
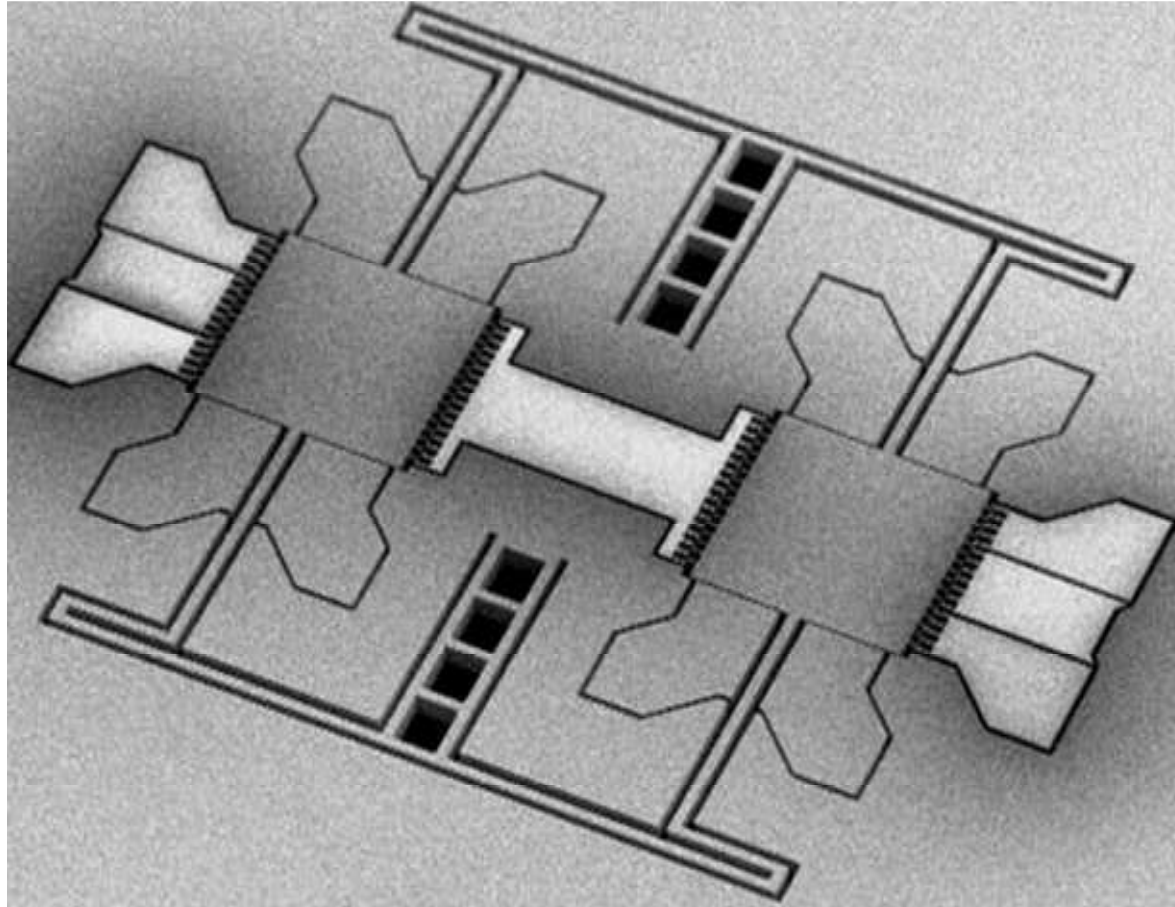
×60

# Principle of Operation

- Coriolis Effect
- Tuning Fork
  - Transfer of energy between two vibration modes
  - Deflection proportional to rotation rate



# Mode-Matched Tuning Fork Gyroscope



- ❑ Fabricated on 60 $\mu$ m thick Silicon-on-insulator (SOI)
- ❑ Fully differential and symmetric

# Performance Scaling

- **Resolution:** Minimum detectable rotation rate

$$\Omega_{min}(Total) = \sqrt{\Omega_{min}(Brownian)^2 + \Omega_{min}(Electronic)^2}$$



$$\Omega_{min}(Brownian) \propto \frac{1}{x_{drive}} \sqrt{\frac{4k_B T}{\omega_0 M Q_{EFF}}}$$

$$\Omega_{min}(Electronic) \propto \frac{\omega_0 V_n}{Q_{EFF}} \left( \frac{\text{sense gap}}{\text{thickness}} \right)$$

- **Scale Factor:** Sensitivity to rotation

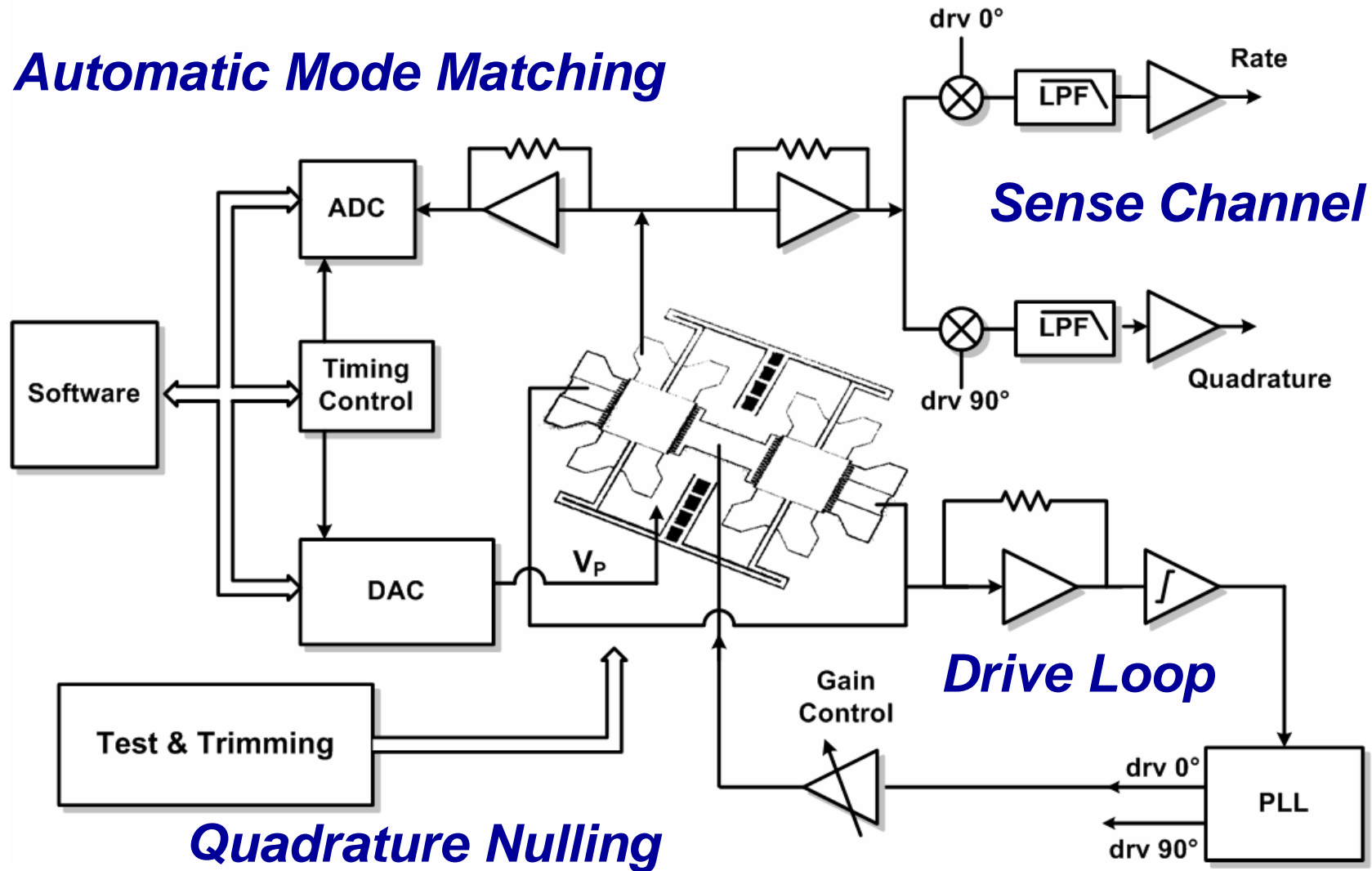
$$S_{OUT} \propto \frac{V_P Q_{EFF}}{\text{sense gap}} \Omega_Z$$

- **Drift:** Long-term accuracy & stability

$$N_B \propto \frac{\omega_0^2}{Q_{EFF}^2 \text{Area}_{electrodes}}$$

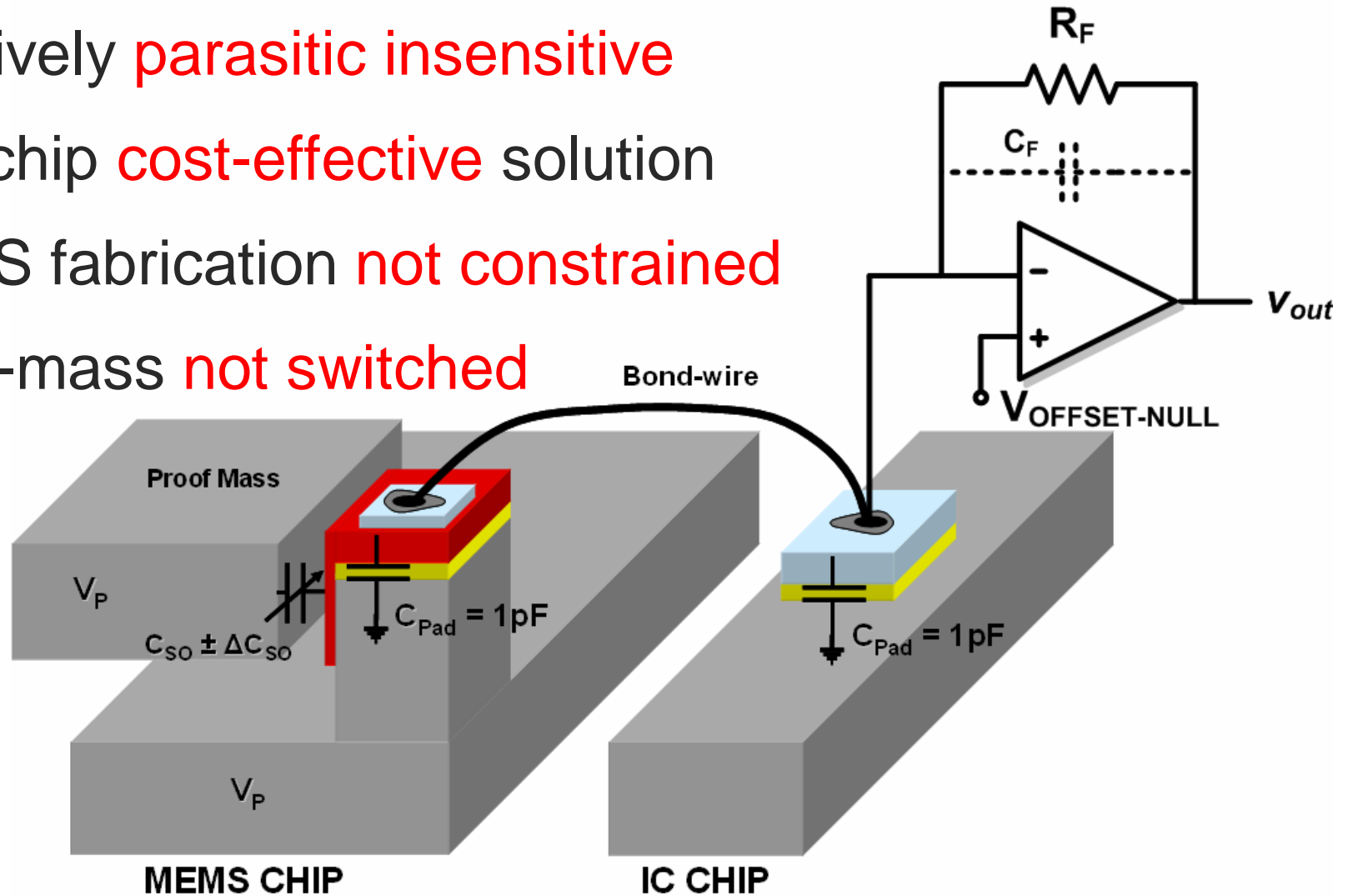
# M<sup>2</sup>-TFG System Electronics

## Automatic Mode Matching



# Transimpedance Amplifier (TIA) Front-end

- Relatively **parasitic insensitive**
- Two-chip **cost-effective** solution
- MEMS fabrication **not constrained**
- Proof-mass **not switched**



# Motional Current and Impedance

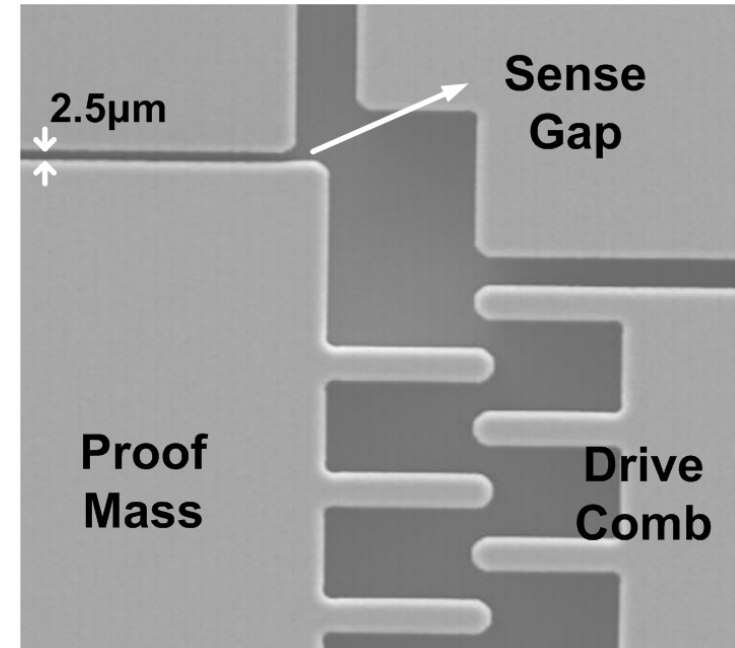
- Current due to input rotation

$$I_{SENSOR} \propto \frac{V_P Q_{sense} q_{drive}}{d_{so}} \Omega_Z$$

**Typical motional current levels**  
**1pA – 1nA**

Implication of large motional impedance

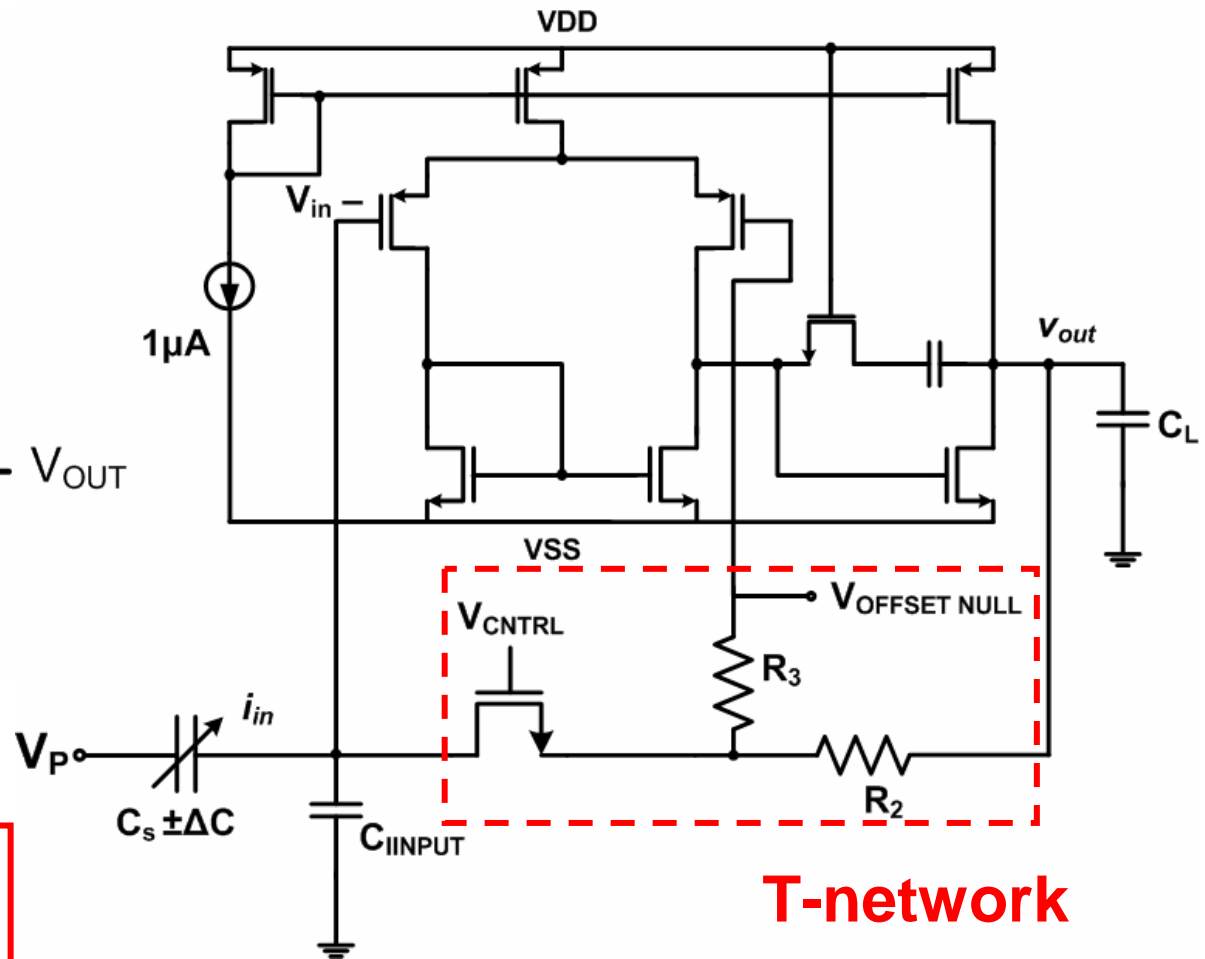
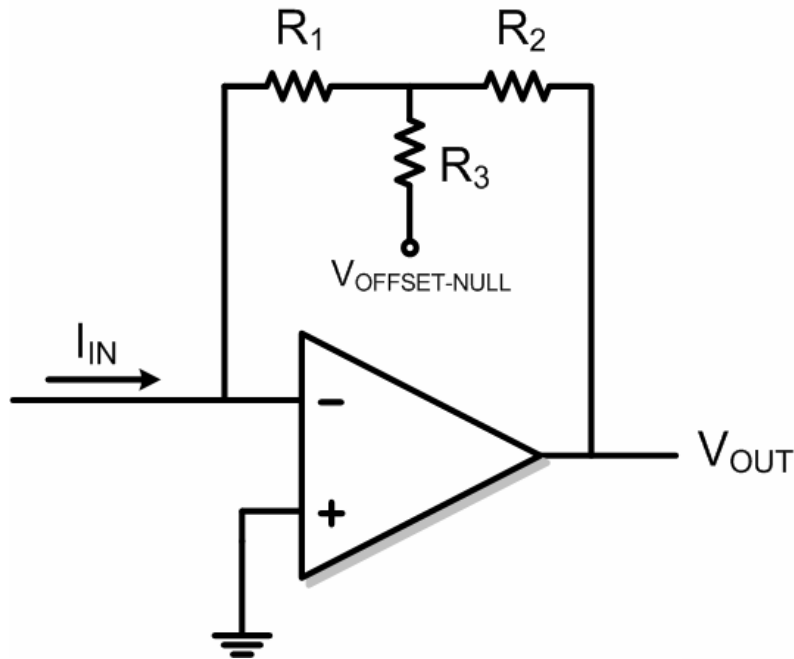
- Higher drive voltages
- Large on-chip transimpedances
- Higher power dissipation



*Close-up of sense gap  
and drive combs*

**Typical Impedance  
values 1 – 10 MΩ**

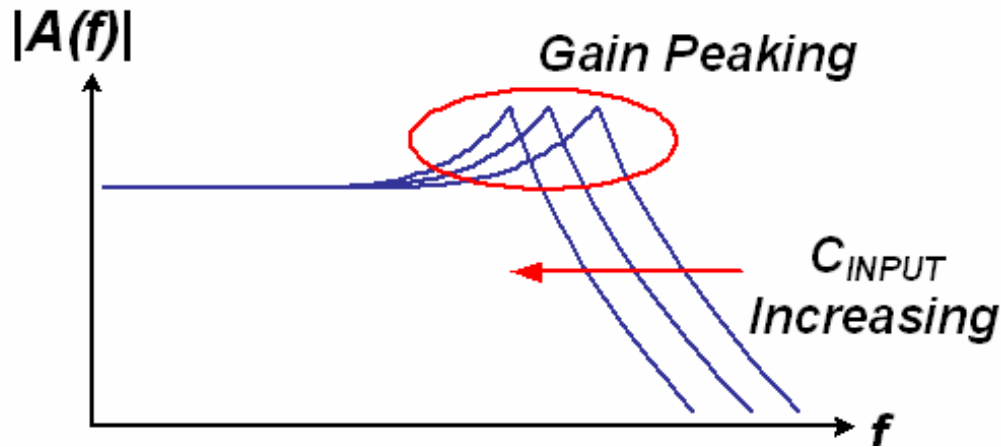
# T-network TIA



**T-network**

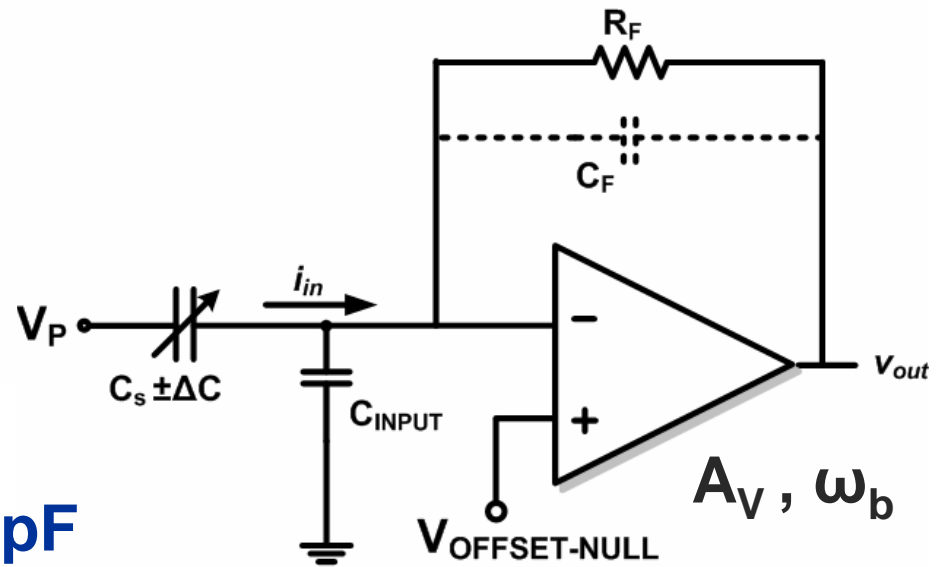
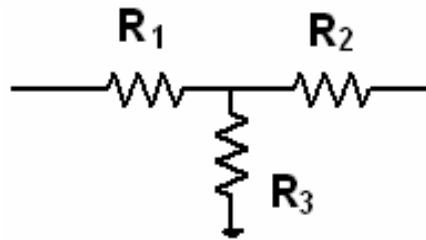
$$\frac{V_{out}}{I_S} = \frac{R_1 R_2}{R_2 \parallel R_3} + R_2$$

# Design Considerations



$$\left. \frac{V_{out}}{i_{in}} \right|_{OL} = \frac{A_v R_F}{\left(1 + \frac{s}{\omega_b}\right) \left(1 + \frac{s}{\omega_{in}}\right)}$$

$$\frac{R_2}{R_3} \leq \frac{C_{INPUT}}{C_F}$$

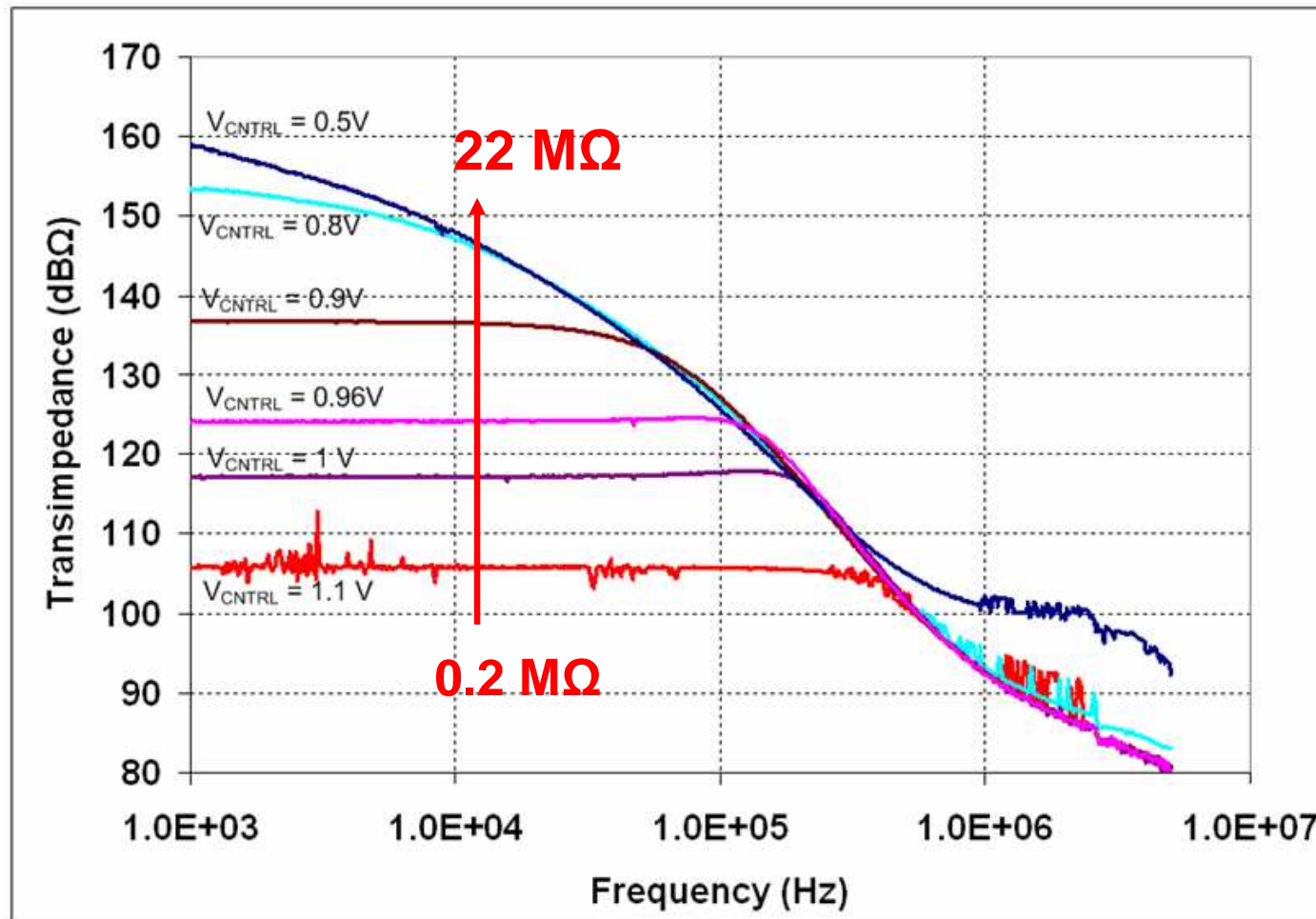


$$C_{INPUT} \sim 2 - 10 \text{ pF}$$

$$C_F \sim 0.5 \text{ pF}$$

# Transimpedance Gain of T-network TIA

- Maximum transimpedance (at 10kHz) ~ 22M $\Omega$

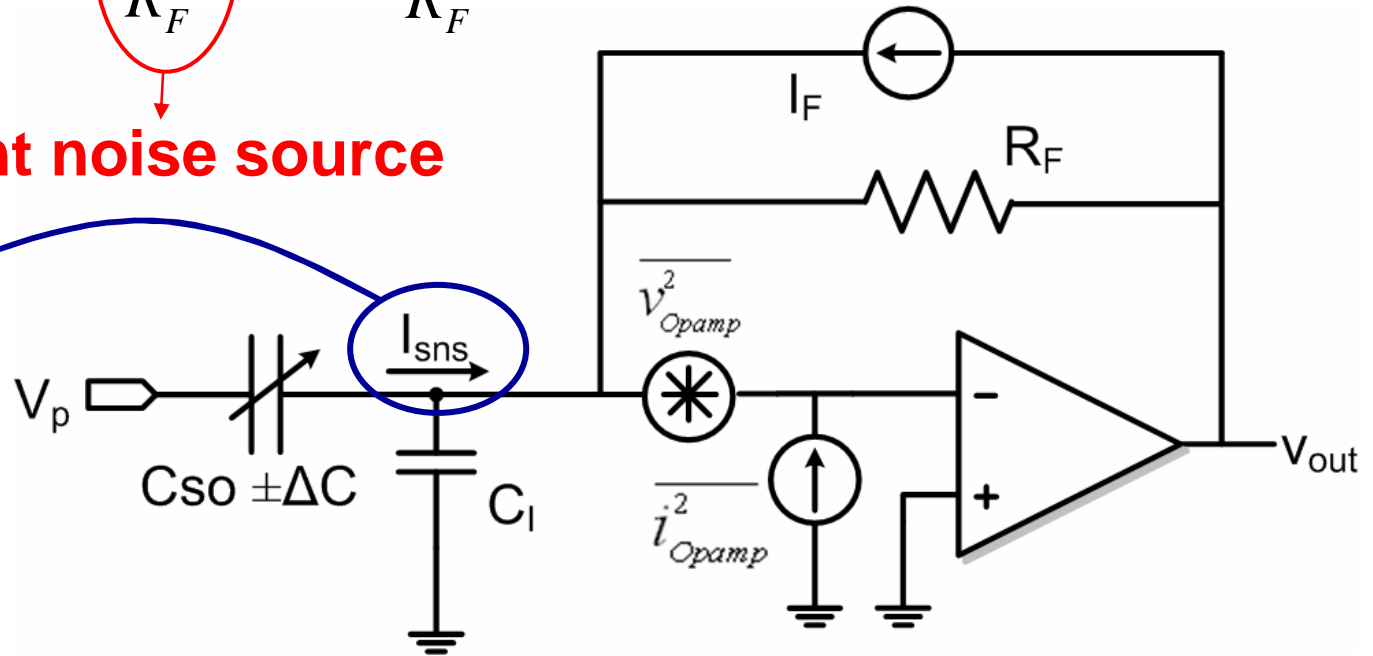


# Noise and SNR in TIAs

$$\overline{i_{TOT}^2} \approx \overline{i_{OPAMP}^2} + \frac{4kT}{R_F} + \frac{\overline{v_{OPAMP}^2}}{R_F^2}$$

$R_F$  is dominant noise source

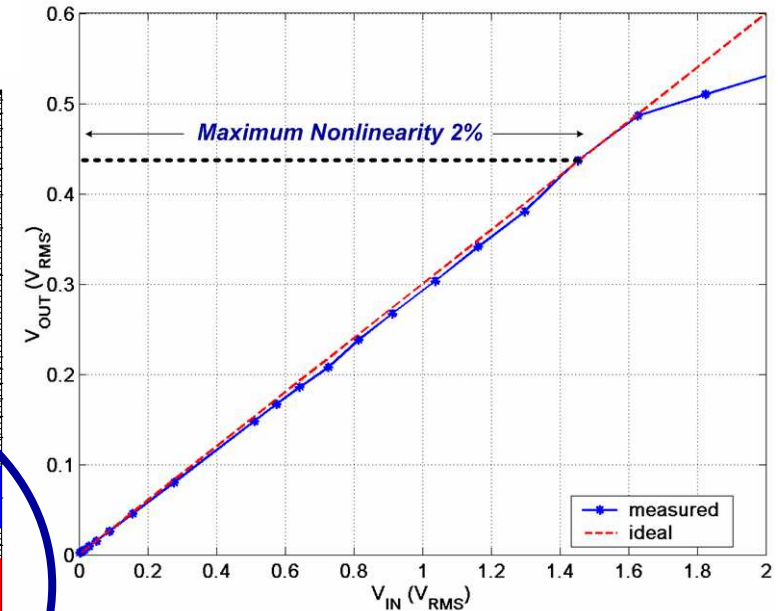
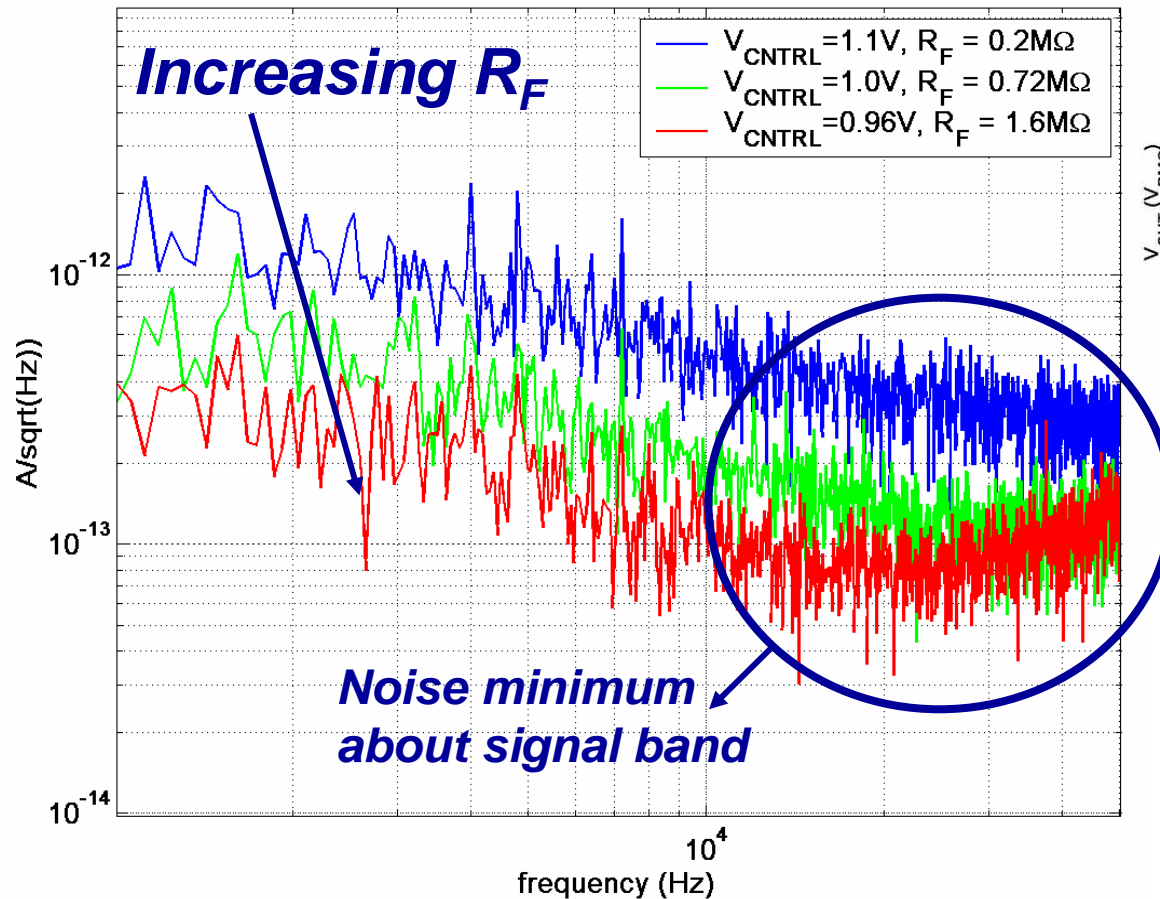
$$i_{in} = V_p \omega_o \Delta C$$



$$SNR = \frac{S_o}{N_o} = \frac{I_{SNS}}{I_{NOISE}} = \frac{I_{SNS} \sqrt{R_F}}{\sqrt{4kT}}$$

# Noise Characterization of the T-network TIA

- Input referred current noise ~  **$88\text{fA}/\sqrt{\text{Hz}}$**  i.e.  $\Delta C_{\text{MIN}} = \mathbf{0.02\text{aF}/\sqrt{\text{Hz}}}$   
(for  $R_F = 1.6\text{M}\Omega$ )

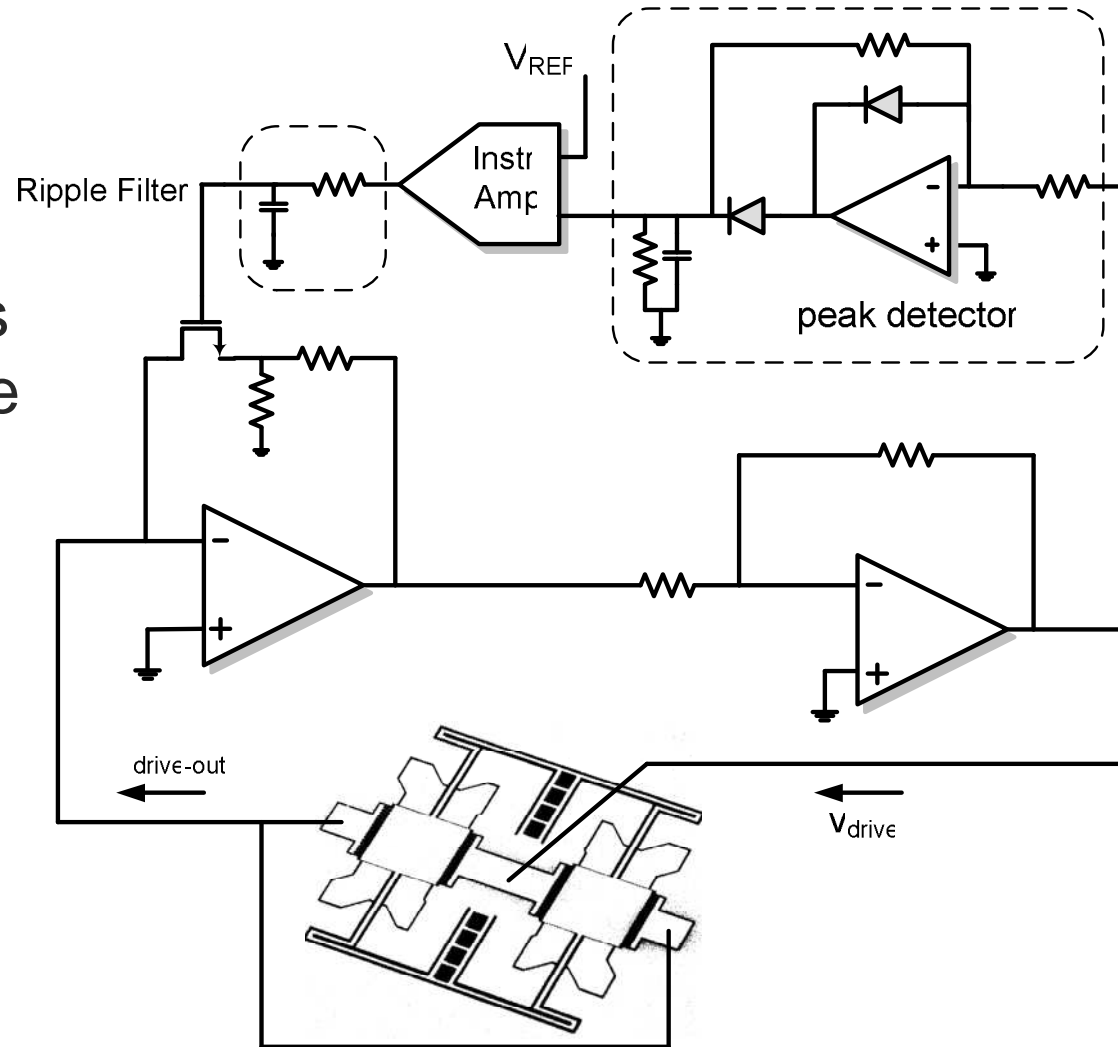


$$DR_{\text{MAX}} = \frac{\text{max output signal}}{\text{noise floor} \times \text{Bandwidth}}$$

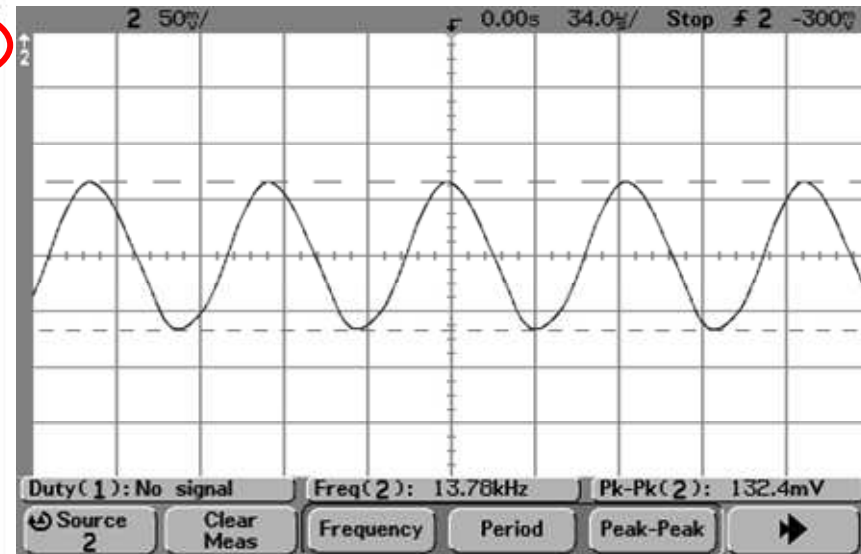
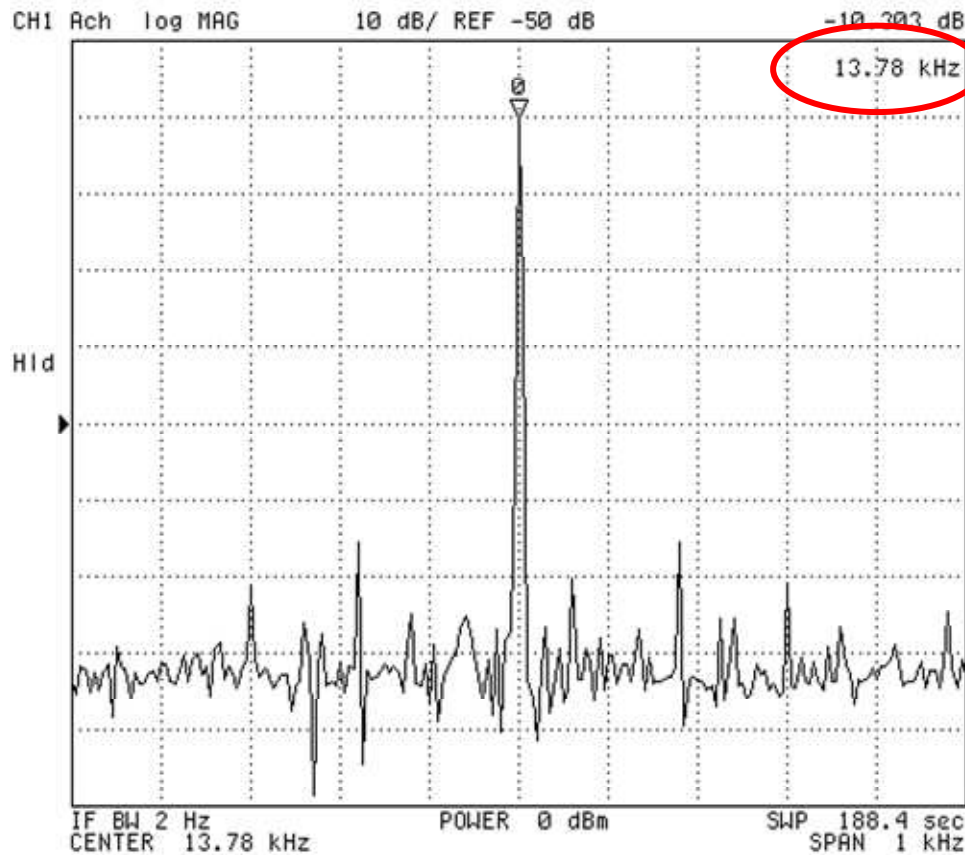
$$DR_{\text{MAX}} \sim 104\text{dB}$$

# Electromechanical Drive Oscillator

- Satisfy **Barkhausen** criteria
- **Automatic Level Control (ALC)** maintains constant drive amplitude



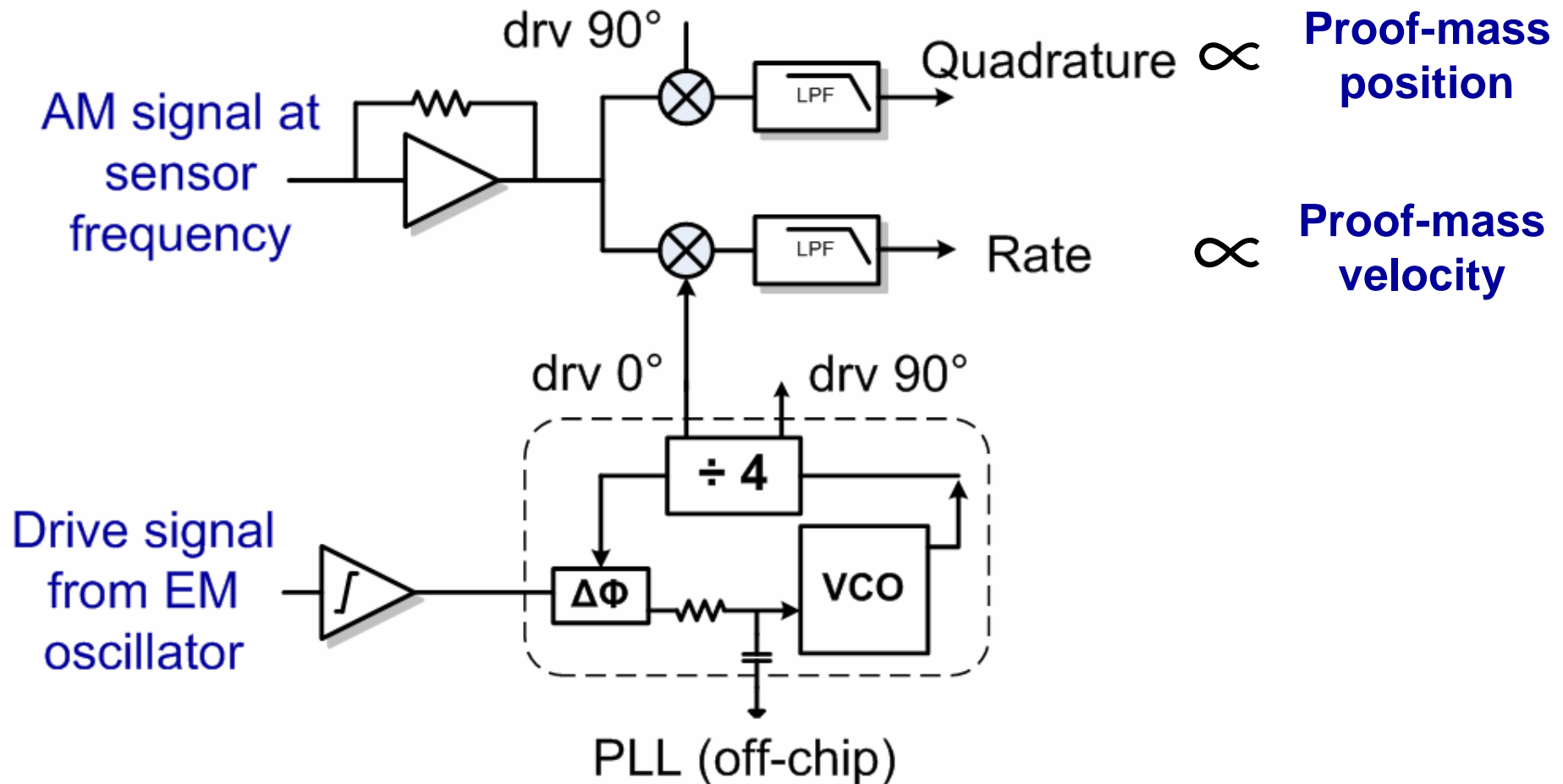
# Drive Oscillator – spectrum and waveform



$$f_{\text{drive}} = 13.78\text{kHz}$$
$$V_{\text{PK-PK}} = 132\text{mV}$$

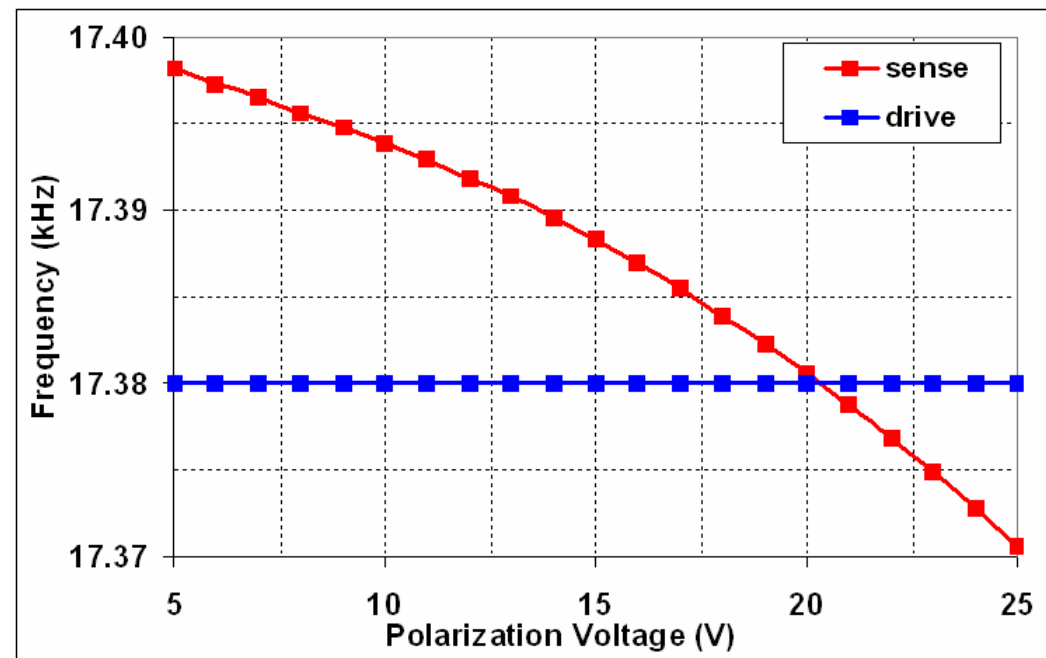
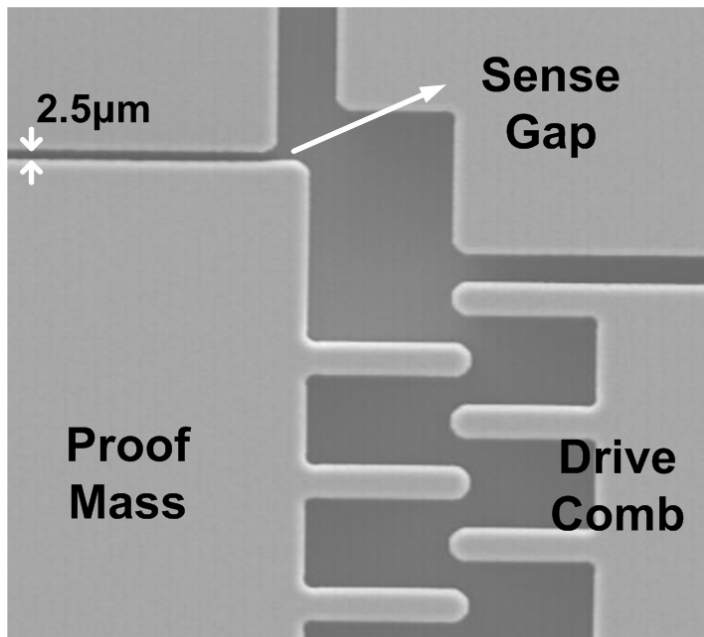
# Rate Sensing

- ❑ **Synchronous I-Q demodulation** extracts rate information



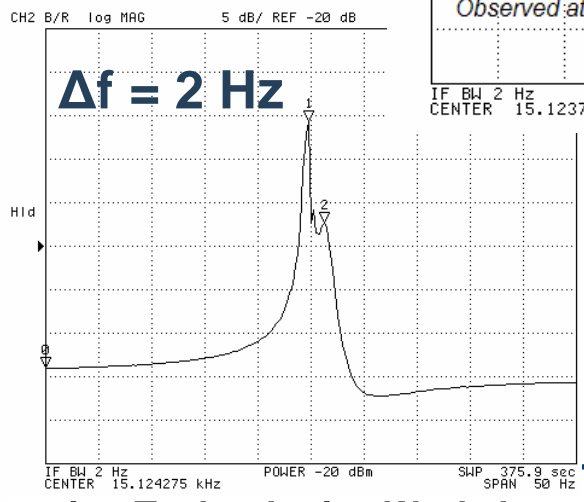
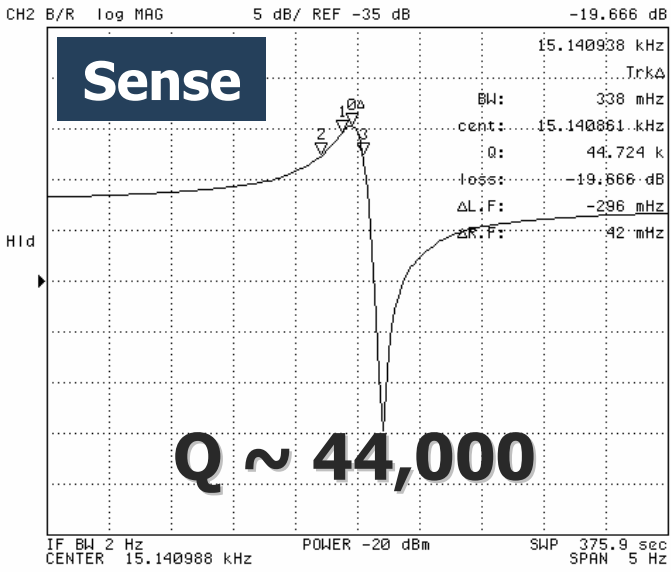
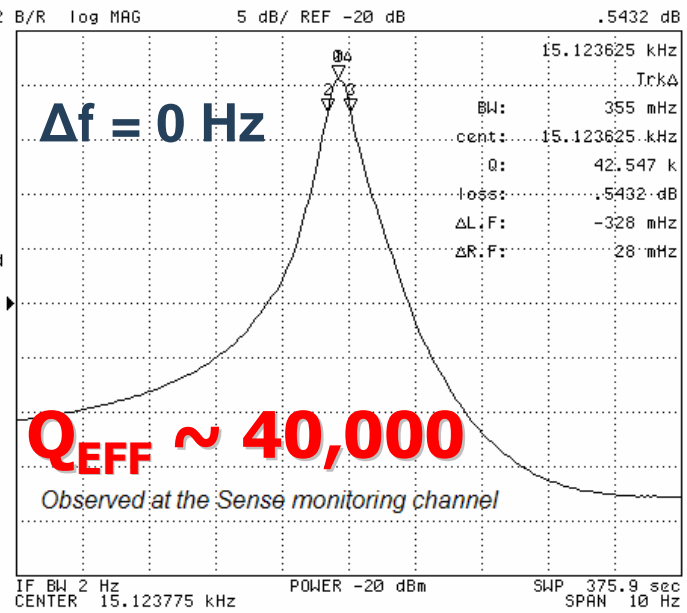
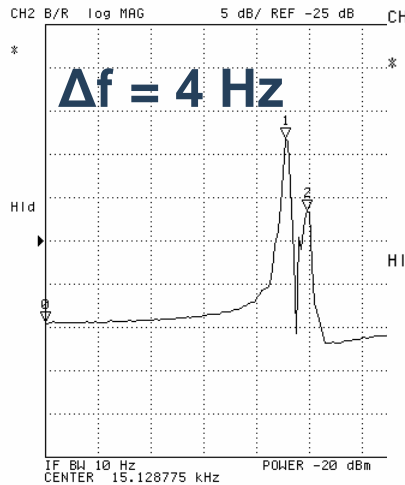
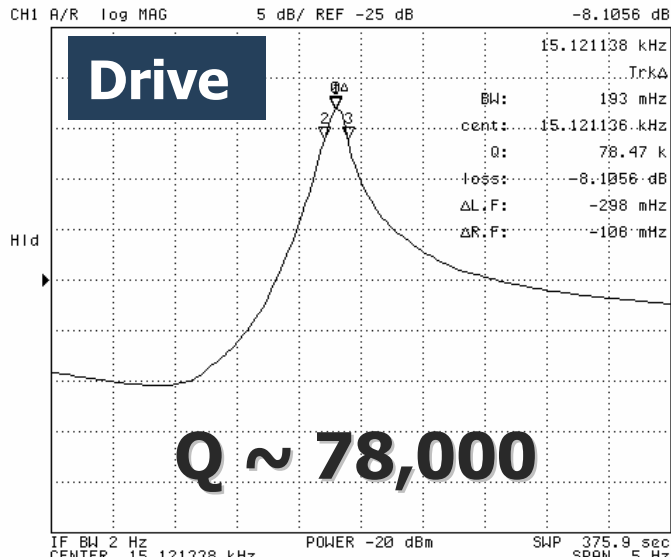
# Electronic Frequency Control

- Electrostatic spring softening allows control of *sense mode frequency only* via DC polarization voltage ( $V_P$ )
- $f_{\text{SENSE}} > f_{\text{DRIVE}} \rightarrow$  Enables tuning despite process variations



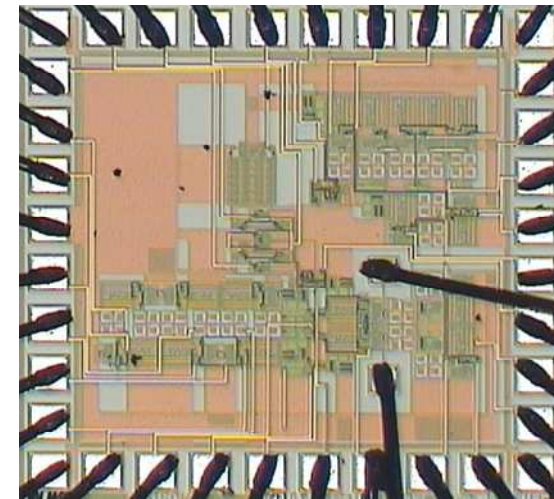
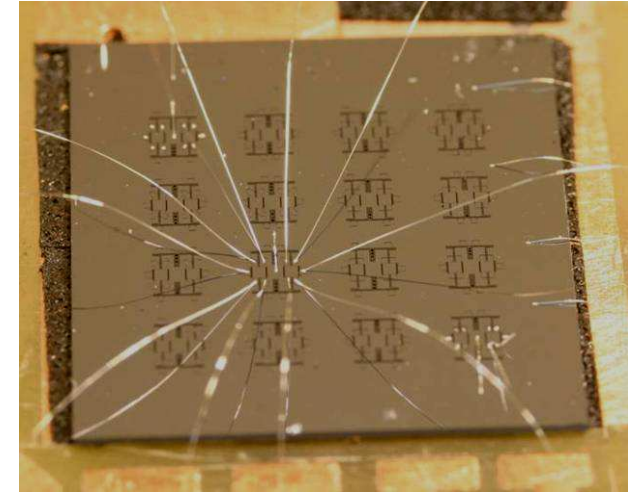
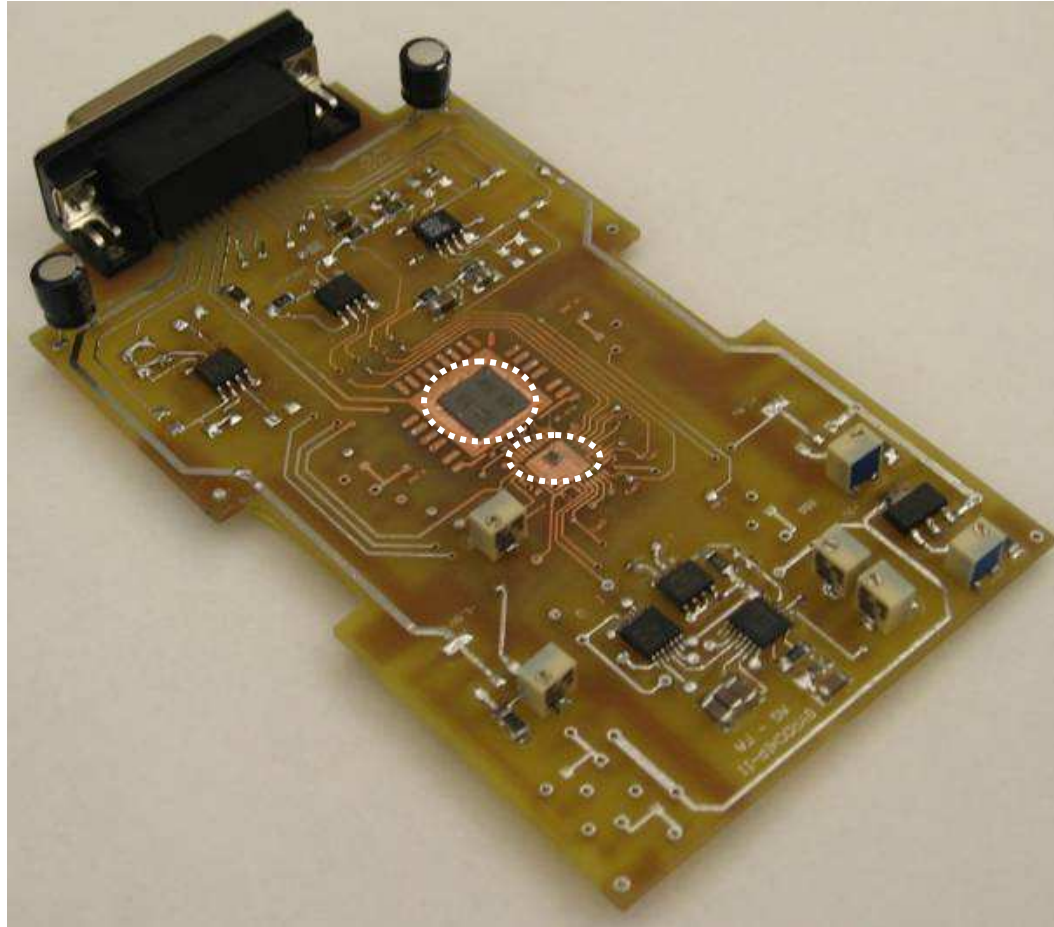
# Resonant Modes and Mode Matching

## Device Mode-Matching

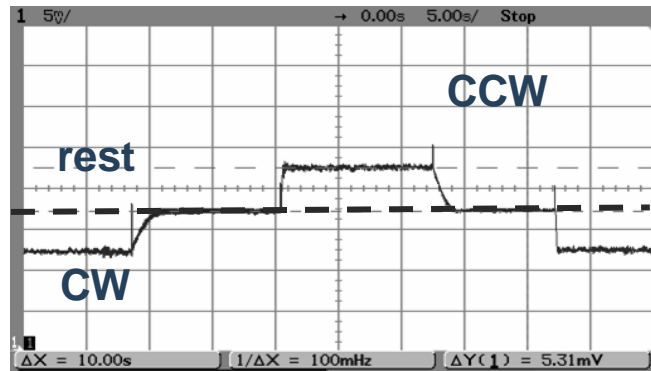


**First reported 0Hz frequency split in non-degenerate vibratory  $\mu$ -Gyro**

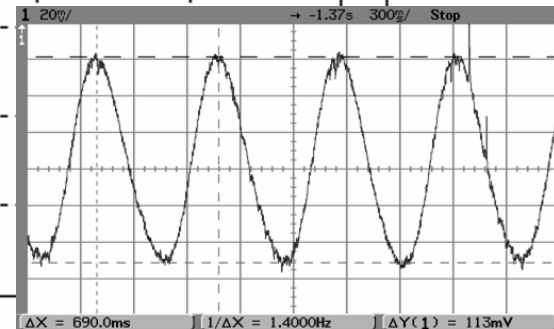
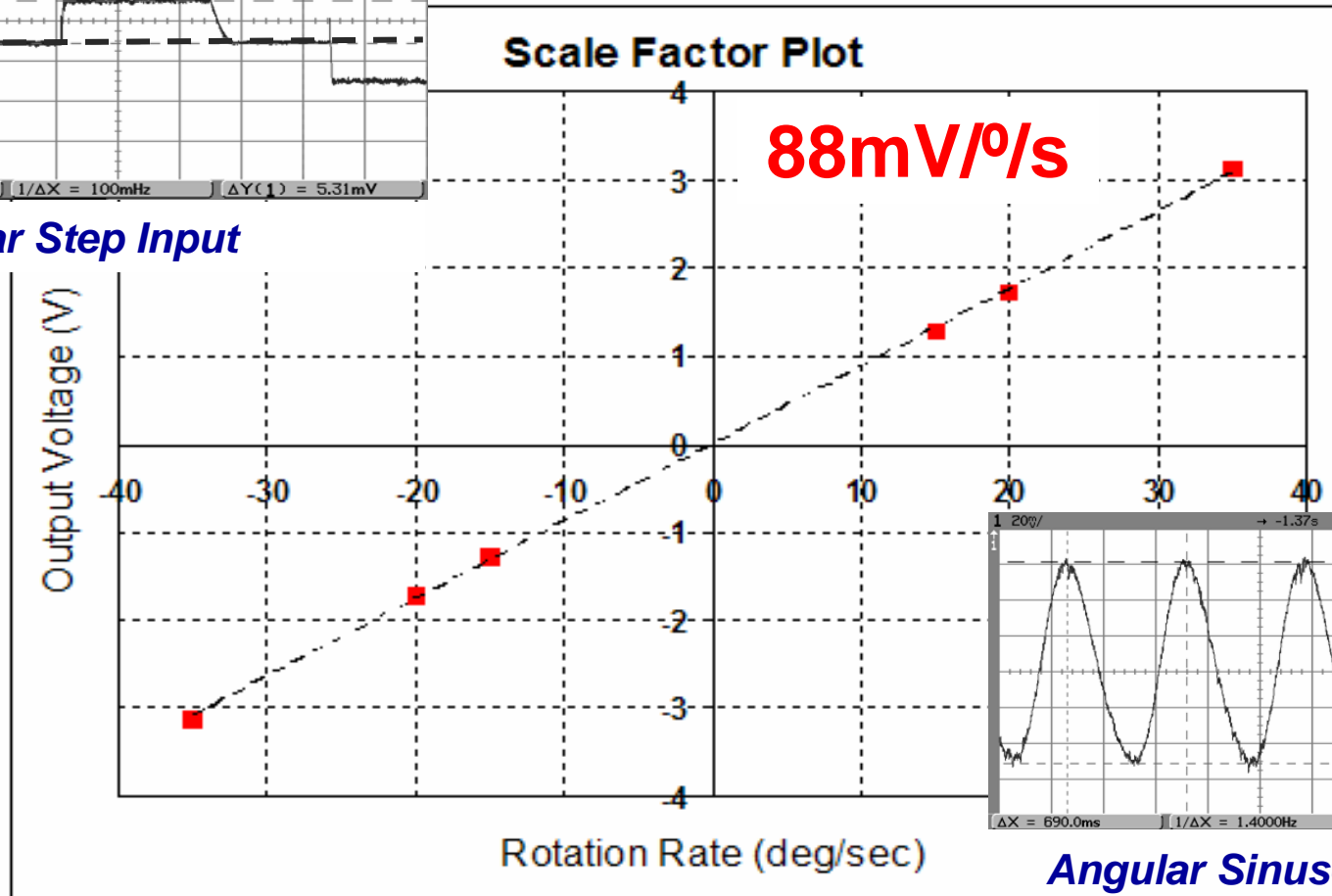
# System Implementation



# Scale Factor Characterization

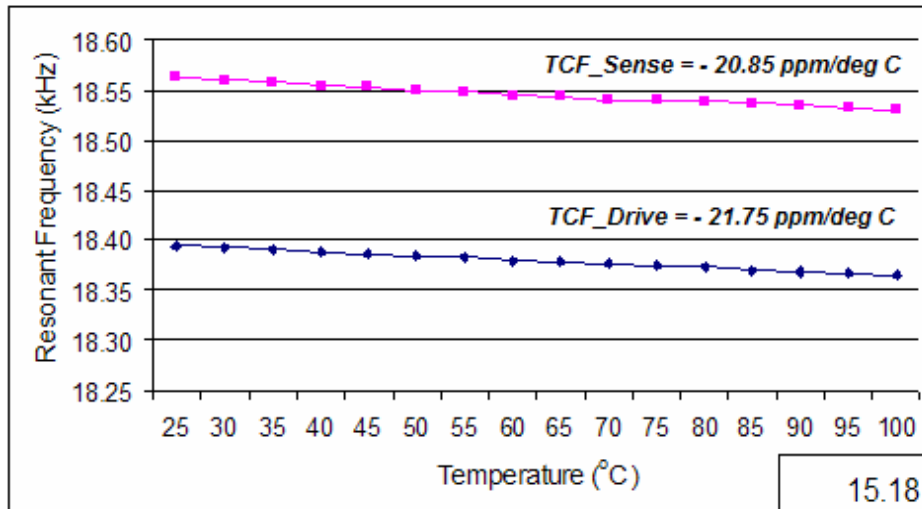


*Angular Step Input*



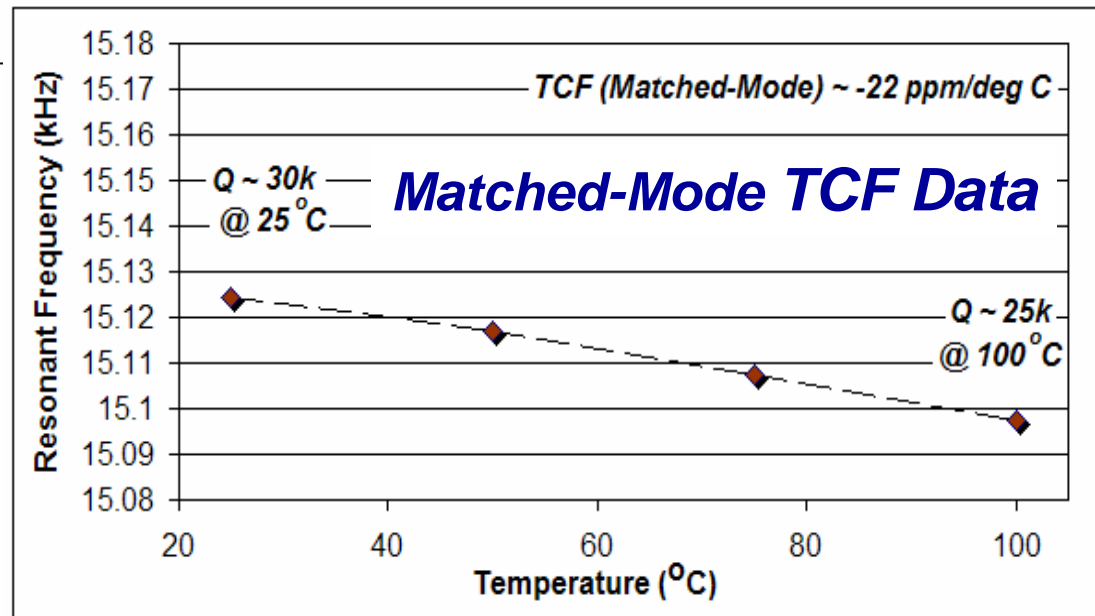
*Angular Sinusoidal Input*

# Temperature Characterization



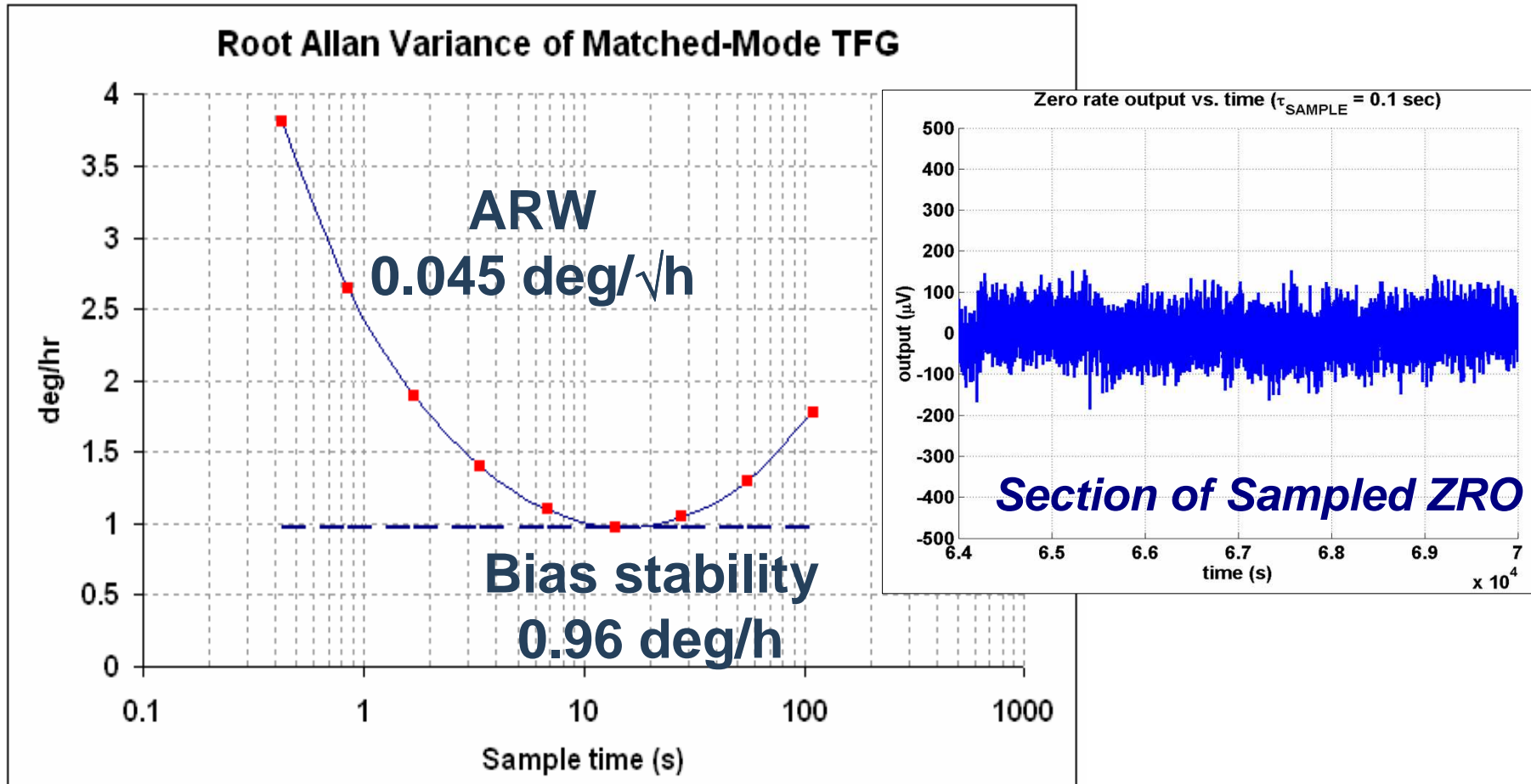
## TCF Data of Individual Modes

**Mode-Matching  
maintained over  
25°C – 100°C**



# Bias Drift Characterization

- Bias drift measured for 12 hours without pre-filtering



# Microsystem Performance Summary

Parameter	Value
Sensor Brownian Noise Floor	0.5 °/hr/ $\sqrt{\text{Hz}}$
<b>Sensor Bias Stability</b>	<b>&lt; 1 °/hr</b>
Capacitive Sensitivity of Gyro	38 aF/°/s
Drive Motional Impedance	>10 M $\Omega$
<b>Min. detectable <math>\Delta C</math></b>	<b>0.02 aF/<math>\sqrt{\text{Hz}}</math></b>
<b>Minimum SNDR of T-network TIA</b>	<b>104 dB</b>
Rate sensitivity of Gyro + IC	2mV/°/s
Supply Voltage	$\pm 1.5$ V
Die Area (0.6 $\mu\text{m}$ CMOS)	2.25 mm <sup>2</sup>
<b>Total power consumption</b>	<b>15 mW</b>

# Conclusions & Future Work

## *Summary:*

- ❑ The Matched-Mode Tuning Fork Gyroscope (**M<sup>2</sup>-TFG**)
- ❑ **T-network TIA** with **0.02aF/√Hz** capacitive resolution and **104dB** linear dynamic range
- ❑ MEMS-based angular rate sensor with **0.5 °/hr/√Hz** noise floor and **< 1°/hr bias drift**

## *Future Work:*

- ❑ Wafer-level vacuum packaging of MEMS devices
- ❑ Process Variation
- ❑ Voltages

# Acknowledgements

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